

Multi-Subregion Based Correlation Filter Bank for Robust Face Recognition

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Abstract

In this paper, we propose an effective feature extraction algorithm, called Multi-Subregion based Correlation Filter Bank (MS-CFB), for robust face recognition. MS-CFB combines the benefits of global-based and local-based feature extraction algorithms, where multiple correlation filters corresponding to different face subregions are jointly designed to optimize the overall correlation outputs. Furthermore, we reduce the computational complexity of MS-CFB by designing the correlation filter bank in the spatial domain and improve its generalization capability by capitalizing on the unconstrained form during the filter bank design process. MS-CFB not only takes the differences among face subregions into account, but also effectively exploits the discriminative information in face subregions. Experimental results on various public face databases demonstrate that the proposed algorithm provides a better feature representation for classification and achieves higher recognition rates compared with several state-of-the-art algorithms.

Keywords: Correlation filter bank, Feature extraction, Face recognition

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1. Introduction

In the past few decades, we have witnessed a rapid development of the theories and algorithms of face recognition and its successful applications in access control, video surveillance, law enforcement, human computer interaction, and so on [1, 2, 3]. However, face recognition is still a very challenging task due to large face appearance variations caused by occlusions, aging, changes of illumination, facial expression, pose, etc. In particular, in many real-world applications, it often suffers from the small sample size (SSS) problem [2] since the training samples of each subject are very few, which can severely affect the performance of most face recognition algorithms especially when the dimension of facial feature space is high.

It has been well recognized that effective feature extraction (FE) plays an important role in the success of a face recognition algorithm [1, 2, 3, 4]. After the FE process, a proper low-dimensional feature vector, with which the class separability is enhanced and the computational complexity of subsequent classifiers is reduced, is generated. FE algorithms can be roughly grouped into two categories [4]: global-based and local-based. Global-based FE algorithms consider a face region as a whole. The extracted features contain the information embedded in the whole face [5]. On the other hand, local-based FE algorithms are based on face subregions (i.e., local facial features, such as eyes, nose, mouth, and chin [4, 6, 7]) and encode the detailed characteristics within each face subregion.

Traditional local-based FE algorithms usually combine the outputs from different face subregions by adopting a fusion strategy (e.g., the majority voting [8], the weighted sum [4, 9, 10], or the concatenation of original/low-dimensional features [11, 12, 13]). Note that the above-mentioned algorithms consider the local FE step and the combination of different subregions as two

independent processes. Although many successful local-based FE algorithms have been proposed, it remains an open issue that how to combine these two processes as a whole.

In this paper, we propose an effective feature extraction algorithm, called Multi-Subregion based Correlation Filter Bank (MS-CFB), for robust face recognition. A new type of filter bank, i.e., Correlation Filter Bank (CFB), is employed in MS-CFB. We formulate the filter bank design as a minimization problem of the generalized Rayleigh quotient [14], which has a closed-form solution. The advantages of this development are the reduction in the computational complexity and the simplification in the decision process, since we can obtain multiple correlation filters corresponding to different face subregions simultaneously.

Compared with traditional algorithms, the proposed MS-CFB algorithm has the following characteristics:

- MS-CFB makes use of local facial features to perform global FE. Therefore, MS-CFB exploits the benefits of both local face subregions and the whole face for extracting features, which incorporates the advantages of both global-based and local-based FE algorithms.
- Traditional local-based FE algorithms consider the local FE step and the combination of different face subregions as two independent processes. In contrast, MS-CFB tries to unify these two processes in an integrated framework. The local FE step of MS-CFB aims to optimize the overall correlation outputs from all face subregions. Such strategy enhances the effectiveness of local feature extraction.
- While conventional correlation filters [15] rely on the frequency domain representations, the design process of a CFB is based on the spatial domain representations, which effectively reduces the computational

complexity during the filter bank design process (this is because the Fourier transforms used in traditional algorithms are not required). Moreover, compared with commonly used constrained correlation filters in face recognition (such as OTF [15]), a CFB is designed by capitalizing on the unconstrained form to improve its generalization capability.

The remainder of this paper is organized as follows. Related work is discussed in Section 2. A detailed description of the proposed MS-CFB algorithm is presented in Section 3. In Section 4, the experimental results on various public face databases are given. Finally, the concluding remarks and future work are provided in Section 5.

2. Related Work

In this section, we begin with reviewing some widely used FE algorithms including popular global-based and local-based FE algorithms in Section 2.1. Some traditional and recently developed correlation filters are described in Section 2.2. The motivation of this work is given in Section 2.3.

2.1. Global-based and Local-based FE Algorithms

A large number of global-based FE algorithms have been developed so far. One of the most successful algorithms for face recognition is appearance-based algorithms, where a face is represented as a vector (e.g., it can be obtained by concatenating each row/column of a face image) [5, 16, 17] or a tensor [18, 19]. In practice, however, a high-dimensional vector or a tensor are too large to allow fast and robust face recognition. A common way to solve this problem is to use dimensionality reduction algorithms, such as Principal Component Analysis (PCA) [5], Linear Discriminant Analysis (LDA) [16, 18], or Class-dependence Feature Analysis (CFA) [20, 21]. Each projection vector

in the projection matrix obtained by PCA (or LDA) tries to represent (or discriminate) all classes in the new feature space. On the other hand, each projection vector obtained by CFA, which is based on the design of the correlation filters, discriminates one class from all the other classes. Fig. 1 shows a comparison of the projection vectors obtained by LDA and CFA for a three-class problem.

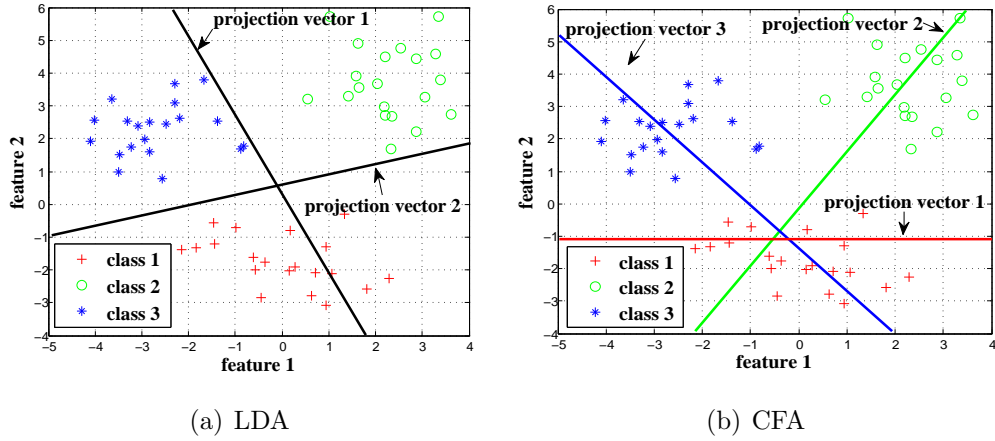


Figure 1: A comparison of the projection vectors obtained by (a) LDA and (b) CFA for a three-class problem. Each projection vector obtained by LDA discriminates all three classes while that obtained by CFA discriminates one class from the other two classes. Note that LDA obtains only two projection vectors.

Global-based FE algorithms, however, do not consider the diversity of local facial structures which can be useful for classification. Recently, local-based FE algorithms have received much attention due to the fact that local facial features (such as eyes and mouth) are more robust to variations of illumination, facial expression, and pose. In [22], the Local Feature Analysis (LFA) algorithm was introduced to encode the local topographic represen-

tations of a face image, where kernels of local spatial support are used to extract information from local face subregions. Kim et al. [11] presented a component-based LDA FE algorithm for image retrieval. Each face subregion is firstly represented as the LDA coefficients in the Fisher subspace. Then, a feature vector is formulated by concatenating all of the coefficients. Finally, a holistic LDA [16], which reduces the dimension of the combined feature vectors, is employed to obtain a compact representation. Li et al. [13] proposed a Block-based Bag Of Words (BBOW) algorithm for robust face recognition. Dense SIFT features [23] are calculated and quantized into different codewords for each face subregion. Then, histograms of each face subregion are concatenated to obtain a feature vector. Finally, linear SVM classifiers are employed to perform classification. Su et al. [4] proposed a novel face recognition algorithm which employs both global and local classifiers. The global feature vector is extracted from a whole face image by using the low frequency Fourier coefficients, while the local feature vector is constructed based on LDA. The final classifier is formed by combining (i.e., using the linear weighted sum) a global feature based classifier and a local feature based classifier. Zhu et al. [8] proposed a Patch-based Collaborative Representation based Classification (PCRC) algorithm for face recognition. The majority voting of the classification outputs from all face subregions is employed to make a final decision. Furthermore, in order to make PCRC less sensitive to the size of face subregions, a multi-scale scheme is used by integrating the complementary information obtained at different scales.

We should point out that, in this paper, we focus on the FE technique, mainly referred to dimensionality reduction [19], which aims to find a mapping from a high-dimensional image space onto a desired low-dimensional face subspace in a global or local manner.

2.2. Correlation Filters

Since the pioneering work by VanderLugt [24], correlation filters have been widely used in signal processing and pattern recognition for decades. One of the most simple correlation filters is the Matched Filter (MF) [24, 25], which uses the complex conjugate of a reference sample. An MF is optimal only when an input sample and the reference sample are identical except that they are with different white noises. However, for practical applications, an input sample suffers from different variations, such as rotations and illumination changes, and thus an MF does not perform well. Therefore, the composite correlation filters [20] were developed instead of a single correlation filter. For instance, Hester et al. [26] proposed the concept of the Synthetic Discriminant Function (SDF) filter, which is the weighted sum of MFs. An SDF filter produces high correlation peaks for authentic samples but it does not consider impostor samples. A Minimum Average Correlation Energy (MACE) filter [27] was proposed to minimize the average energy of a correlation plane for all samples while constraining the correlation outputs for authentic samples. However, an MACE filter emphasizes high frequency parts of samples, which makes it susceptible to noise. An Optimal Tradeoff Filter (OTF) [28] was designed by combining a Minimum Variance Synthetic Discriminant Function (MVSDF) filter [29] (focusing on the low frequency parts of samples) and an MACE filter. Yan et al. [21] proposed an Optimal Extra-class Output Tradeoff Filter (OEOTF) to emphasize the outputs for extra-class samples.

2.3. Motivation

Recent studies [1, 4] have suggested that a hybrid-based FE algorithm, which makes use of both global-based and local-based FE algorithms, could potentially offer the best of the two types of algorithms. Hence, in this paper

we combine global-based and local-based FE algorithms in a principled way. Here, instead of extracting local facial features separately and then combining them by using the weighted sum or the majority voting, the proposed algorithm directly extracts a global feature vector based on the combination of local features. Meanwhile, the local FE steps for different face subregions are jointly performed so that the overall correlation outputs from all face subregions satisfy the design criterion.

On the other hand, to adapt to the correlation filter which is specifically designed for the face recognition task, instead of optimizing the whole correlation plane, we propose to optimize the origin peaks in the correlation plane. This improvement is motivated by the fact that the proposed feature extraction framework mainly considers the information of the origin peaks. One merit of working on the origin peaks is that traditional Fourier transforms are not required (based on the generalized Parseval’s theorem [30]), which improves the computational efficiency during the design process.

3. Multi-Subregion Based Correlation Filter Bank (MS-CFB)

In this section, an overview of the proposed MS-CFB algorithm for face recognition is introduced in Section 3.1. The detailed design process of a CFB and feature extraction based on CFBs are described in Sections 3.2 and 3.3, respectively. Classification rule is presented in Section 3.4. The complete algorithm is given in Section 3.5. We discuss the proposed algorithm in Section 3.6.

Before formally presenting the proposed algorithm, we begin by introducing the notations used in this paper. Light case symbols represent the spatial domain while bold case ones refer to the frequency domain.

3.1. Overview of the MS-CFB Algorithm for Face Recognition

An overview of the proposed MS-CFB algorithm for face recognition is shown in Fig. 2.

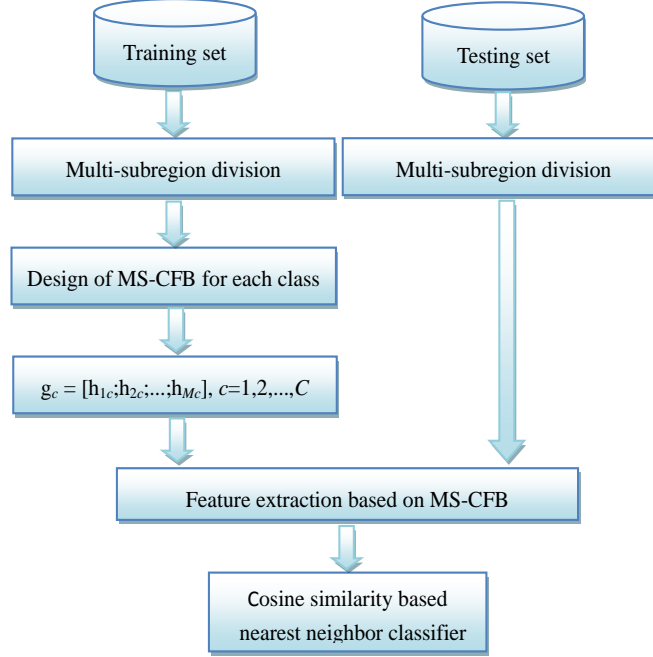


Figure 2: An overview of the MS-CFB algorithm for face recognition.

Inspired by CFA [20, 21], the proposed algorithm tries to distinguish one class from all the other classes for each projection vector. During the training stage, for each face image in the training set, it is firstly divided into multiple blocks of the same size (corresponding to different face subregions). Each face subregion is represented as a high-dimensional vector by concatenating the pixel values in the subregion (other face feature representations, such as SIFT [23] and Gabor [31], can also be used). Secondly, a set of Correlation Filter Banks (CFBs) is designed for all classes (see Section 3.2) and then used to perform feature extraction (see Section 3.3). More specifically, a class-specific

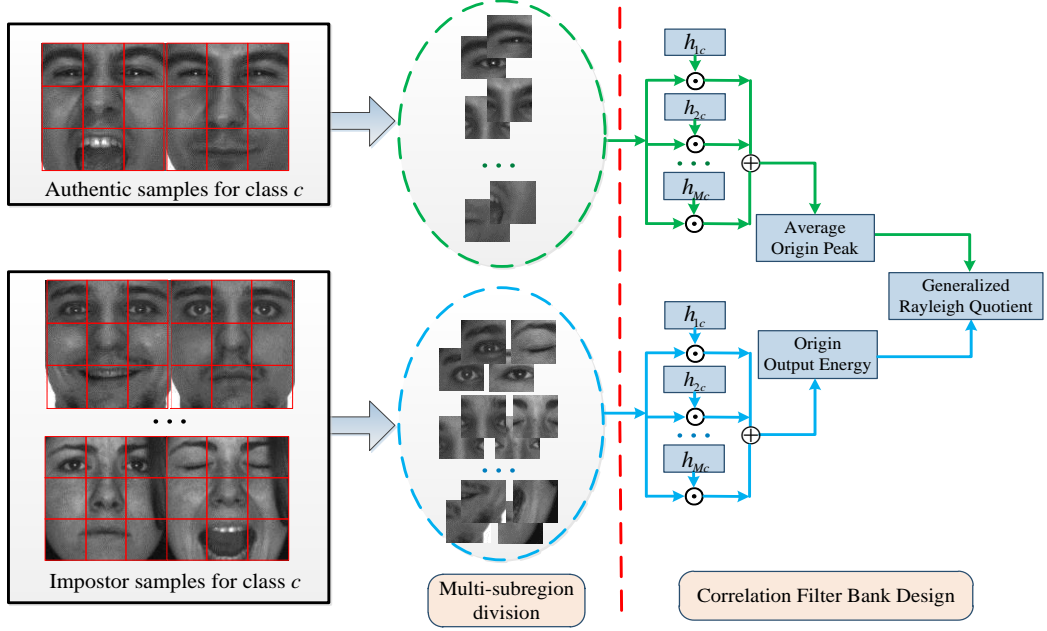


Figure 3: The design process of a CFB. ‘ \odot ’ represents the inner product.

CFB is designed for each class in the training set to discriminate that class from all the other classes, and thus a set of class-specific CFBs is obtained for all classes and employed to extract features. During the test stage, for a face image in the test set, after the multi-subregion division procedure, a feature vector is extracted based on CFBs. Finally, a nearest neighbor classifier is employed for classification.

3.2. Design Process of a CFB

Assume that there are N training images and C classes in the training set. We aim to design a CFB for class c ($c = 1, 2, \dots, C$). The design process of a CFB for class c is shown in Fig. 3.

First, we define the overall correlation output ($O[n]$) of a CFB as:

$$O[n] = \sum_{m=1}^M (x_m \otimes h_{m,c})[n], \quad (1)$$

where x_m is the raw feature vector of the m -th face subregion; $h_{m,c}$ is a correlation filter corresponding to the m -th face subregion for class c ; M is the number of face subregions in a face image; ' \otimes ' stands for the correlation operator.

According to the Fourier transform theory [30], the above equation can be re-written in the frequency domain, that is:

$$O[n] = \sum_{m=1}^M \sum_{k=0}^{D-1} (\mathbf{X}_m[k])^* \mathbf{H}_{m,c}[k] e^{\frac{j2\pi kn}{P}}, \quad (2)$$

where $\mathbf{X}_m[k]$ and $\mathbf{H}_{m,c}[k]$ are the Fourier transforms of x_m and $h_{m,c}$, respectively; ' $*$ ' denotes the conjugate operator; n and k represent the indexes in the spatial domain and frequency domain, respectively; D is the dimension of the raw local facial feature vector. Note that the point $O[0]$, which is equal to the sum of the inner products between the inputs and the correlation filters, is usually referred to the overall origin correlation output or the overall origin peak.

In the CFB, all of the correlation filters are jointly designed so that the outputs for authentic training samples (refer to the training samples in class c) and the ones for impostor training samples (refer to the training samples that are excluded from class c) are well separated. To achieve this goal, we emphasize the outputs for authentic training samples while at the same time, suppressing the outputs for impostor training samples. Formally, the design criterion of a CFB is to minimize the overall origin output energy for impostor training samples and simultaneously maximize the average overall origin peak for authentic training samples for the class of interest.

According to Eq. (2), the overall origin output energy (\mathbb{E}_I) for impostor training samples of class c can be derived as:

$$\begin{aligned}\mathbb{E}_I &= \frac{1}{N_c^I} \sum_{i=1}^{N_c^I} |O_{i,c}^I[0]|^2 \\ &= \frac{1}{N_c^I} \sum_{i=1}^{N_c^I} \left| \sum_{m=1}^M \sum_{k=0}^{D-1} (\mathbf{X}_{mi,c}^I[k])^* \mathbf{H}_{m,c}[k] \right|^2,\end{aligned}\quad (3)$$

where $O_{i,c}^I[0]$ represents the overall origin correlation output corresponding to the i -th impostor training sample of class c ; $\mathbf{X}_{mi,c}^I[k]$ is the Fourier transform of $x_{mi,c}^I$ (see the definition below); N_c^I is the number of impostor training samples of class c .

Based on the generalized Parseval's theorem [30] (which shows that the correlation of two functions is equal to the product of the individual Fourier transforms of the functions, where one of them is complex conjugated), in Eq. (3) we can replace the representations of features in the frequency domain with those in the spatial domain. Therefore, the right side of Eq. (3) is equivalent to the following equation:

$$\begin{aligned}\frac{1}{N_c^I} \sum_{i=1}^{N_c^I} \left| D \sum_{m=1}^M \sum_{n=0}^{D-1} x_{mi,c}^I[n] h_{m,c}[n] \right|^2 &= \frac{D^2}{N_c^I} \sum_{i=1}^{N_c^I} \left| \sum_{m=1}^M h_{m,c}^T x_{mi,c}^I \right|^2 \\ &= \frac{D^2}{N_c^I} \sum_{i=1}^{N_c^I} g_c^T (X_{i,c}^I) (X_{i,c}^I)^T g_c \\ &= g_c^T \Sigma_c g_c,\end{aligned}\quad (4)$$

where $x_{mi,c}^I = (x_{mi,c}^I[0], x_{mi,c}^I[1], \dots, x_{mi,c}^I[D-1])^T$ is the raw feature vector corresponding to the m -th face subregion of the i -th impostor training sample of class c ; $h_{m,c} = (h_{m,c}[0], h_{m,c}[1], \dots, h_{m,c}[D-1])^T$ is the corresponding correlation filter; $X_{i,c}^I = (x_{1i,c}^I; x_{2i,c}^I; \dots; x_{Mi,c}^I) \in R^{MD \times 1}$ is a column vector, which contains M different face subregions of the i -th impostor training

sample; $g_c = (h_{1,c}; h_{2,c}; \dots; h_{M,c}) \in R^{MD \times 1}$ is composed of M correlation filters corresponding to M face subregions, and

$$\Sigma_c = \frac{D^2}{N_c^I} \sum_{i=1}^{N_c^I} (X_{i,c}^I)(X_{i,c}^I)^T, \quad (5)$$

where Σ_c is the covariance matrix which effectively encodes the relationships among M different face subregions.

The average overall origin peak (\mathbb{P}_A) for authentic training samples of class c can be expressed as:

$$\begin{aligned} \mathbb{P}_A &= \frac{1}{N_c} \sum_{j=1}^{N_c} O_{j,c}^A[0] \\ &= \frac{D}{N_c} \sum_{j=1}^{N_c} \sum_{m=1}^M \sum_{n=0}^{D-1} x_{mj,c}^A[n] h_{m,c}[n], \end{aligned} \quad (6)$$

where $O_{j,c}^A[0]$ represents the overall origin correlation output corresponding to the j -th authentic training sample of class c ; N_c is the number of authentic training samples of class c .

Using the vector representation, the right side item of Eq. (6) can be converted as:

$$\begin{aligned} \frac{D}{N_c} \sum_{j=1}^{N_c} \sum_{m=1}^M \sum_{n=0}^{D-1} x_{mj,c}^A[n] h_{m,c}[n] &= \frac{D}{N_c} \sum_{j=1}^{N_c} \sum_{m=1}^M h_{m,c}^T x_{mj,c}^A \\ &= \frac{D}{N_c} \sum_{j=1}^{N_c} (X_{j,c}^A)^T g_c \\ &= m_c^T g_c, \end{aligned} \quad (7)$$

where $x_{mj,c}^A = (x_{mj,c}^A[0], x_{mj,c}^A[1], \dots, x_{mj,c}^A[D-1])^T$ is the raw feature vector corresponding to the m -th face subregion of the j -th authentic training sample of class c ; $X_{j,c}^A = (x_{1j,c}^A; x_{2j,c}^A; \dots; x_{Mj,c}^A) \in R^{MD \times 1}$ is a column vector,

which contains M different face subregions of the j -th authentic training sample, and

$$m_c = \frac{D}{N_c} \sum_{j=1}^{N_c} X_{j,c}^A, \quad (8)$$

where m_c is the mean of all authentic training samples of class c .

Therefore, in order to maximize the average overall origin peak for authentic training samples while minimizing the overall origin output energy for impostor training samples, we employ the quotient form by combining Eqs. (4) and (7), that is,

$$J(g_c) = \frac{\mathbb{P}_A^2}{\mathbb{E}_I} = \frac{|m_c^T g_c|^2}{g_c^T \Sigma_c g_c}. \quad (9)$$

As we can see, $J(g_c)$ is the generalized Rayleigh quotient [14] which reaches its maximal value when Σ_c is a non-singular matrix. Unfortunately, recalling that $\Sigma_c = \frac{D^2}{N_c^I} \sum_{i=1}^{N_c^I} (X_{i,c}^I)(X_{i,c}^I)^T$, where $X_{i,c}^I \in R^{MD \times 1}$, it is easy to derive that $\Sigma_c \in R^{MD \times MD}$ is a singular matrix since $\text{rank}(\Sigma_c) \leq N_c^I$ (by using the properties of the rank) and $N_c^I \ll MD$ (i.e., the SSS problem). Therefore, to resolve the singularity problem of Σ_c , we add a regularized term to Eq. (9). As a result, the optimization criterion becomes

$$g_c = \arg \max_{g_c} \frac{|m_c^T g_c|^2}{g_c^T \hat{\Sigma}_c g_c}. \quad (10)$$

Here $\hat{\Sigma}_c = (1 - \alpha)\Sigma_c + \alpha\mathbb{I}$, where $\alpha \in [0, 1]$ is the regularized parameter and $\mathbb{I} \in R^{MD \times MD}$ is an identity matrix.

Based on some matrix operations [14], the solution of Eq. (10) is

$$g_c = \hat{\Sigma}_c^{-1} m_c. \quad (11)$$

Once g_c is computed, all of the correlation filters $h_{m,c}$ ($m = 1, 2, \dots, M$) can be obtained simultaneously for class c . In this paper, g_c is termed as

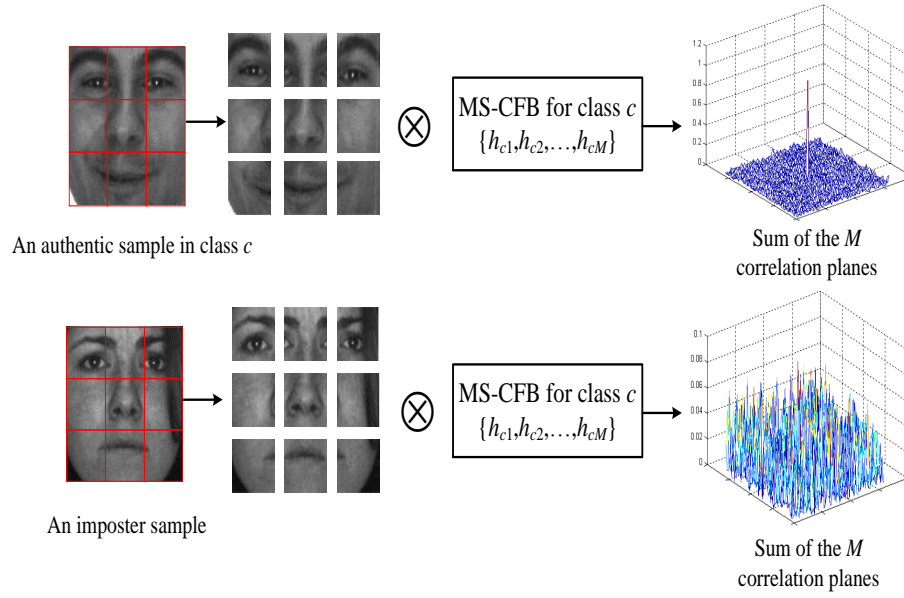


Figure 4: The correlation outputs of a CFB for an authentic test sample and an imposter one.

the Correlation Filter Bank (CFB), since it consists of multiple correlation filters corresponding to different face subregions. Fig. 4 illustrates the typical correlation outputs of a CFB for an authentic test sample and an impostor one. As shown in Fig. 4, for an authentic test sample, the CFB can produce a sharp peak, while the correlation output has no discernible peak for an impostor test sample.

The time complexity to design a CFB is $O(N_c^I(MD)^2 + (MD)^3 + MD)$, where M and D are the number of face subregions and the dimension of local facial feature space, respectively. N_c^I is the number of impostor training samples of class c . The time cost mainly comprises three parts: $O(N_c^I(MD)^2)$ is used to compute $\hat{\Sigma}_c$; $O((MD)^3)$ is used to calculate the matrix inversion of $\hat{\Sigma}_c$; and $O(MD)$ is used to construct the final g_c . Therefore, the non-diagonal matrix inversion of $\hat{\Sigma}_c$ consumes the majority time during the design process of a CFB.

3.3. Feature Extraction Based on CFBs

After obtaining a set of CFBs (a CFB is designed by optimizing Eq. (10) for one class) during the training stage, we can perform feature extraction for both training set and test set. A face image correlated with all CFBs generates a features vector to represent the image.

The proposed framework of feature extraction based on CFBs is illustrated in Fig. 5. According to Fig. 5, the sum of the correlation outputs is first computed for each CFB. A global feature vector, which exploits the statistics of local face subregions, is then constructed based on the origin correlation outputs of all CFBs. To be specific, after the multi-subregion division procedure, a raw feature vector is first extracted for each face subregion. Next, the correlations between the correlation filters in the CFB and the corresponding raw feature vectors are calculated and then summed for

1 课题背景和课题简介（主要是视频监控系统的背景和意义）

随着我国社会经济的不断发展，地区之间的人员流动日益频繁。随之出现了一系列的安全问题，许多违法犯罪分子流窜作案，跨地区的犯罪呈上升趋势，这给国家治安和社会治安的长久稳定带来了严重的问题。为了保障城市的社会治安和稳定，许多城市采用了电子化的视频监控系統。利用视频监控系統来抓捕危险的犯罪分子和预防各类可能的重大突发事件是一种有效抑止跨地区犯罪和维护社会治安的方式。但是现有的视频监控系統主要还是基于人工的运作方式。凭借人工进行嫌疑人或者各类突发事件的查找和识别，浪费了大量的劳力和物力。如何进行智能化的监控和利用先进的模式分析和识别技术，特别是自动的目标检测，跟踪和识别技术（包括人脸识别，行为识别等）分析各类突发事件或者嫌疑人对于保障国家和社会安全具有十分重要的意义。另一方面，硬件水平的不断发展和模式分析和识别技术的不断进步也给智能化目标识别带来了巨大的市场应用前景。在视频智能监控，生物特征认证，信息安全和人机交互等领域目标检测，跟踪和识别技术都具有巨大的应用潜力。

现在我国电子政务建设中的重点业务系統就是“平安城市”。在“平安城市”的建设中，其核心是城市报警与监控系统，城市报警与监控系统建设也是社会治安防控体系的重要组成部分。公安部2004年在全国范围内确定了22个城市作为首批科技强警示范城市。2005年确定中西部地区的15个城市和江苏、浙江、山东、广东四省的23个城市作为第二批示范城市。2007至2008年，则为第三批示范城市建设的时期，到2008年，科技强警示范城市已经达到180个。“平安城市”的建设促进了视频监控市场的迅速增长，到2008年，全国约有200万个监控摄像头用于城市监控与报警系統。可以看出视频监控市场巨大。以往依靠单纯的人力已经无法应付上万人的数据库查询和分析工作。基于视频监控系统的目标检测，跟踪和识别具有重要的经济意义和社会意义。

综上所述，该项目具有巨大的经济效益和社会效益，是一项亟待开展的研究课题。

// <下面主要是针对人脸识别的背景和意义>

硬件水平的不断发展和人脸识别技术的不断进步给人脸识别带来了巨大的市场应用前景。在视频智能监控，生物特征认证，信息安全和人机交互等领域人脸识别都具有巨大的应用潜力。同时各国政府也在大力发展包括人脸识别在内的各种生物特征识别技术。9·11以后，以美国为首的西方世界各国都将生物特征识别技术作为关系国家未来安全的重大关键技术加以扶持。在国外，美国在911后连续发布三个法案强调在边检、执法、民用航空等领域应用包括人脸识别在内的生物特征识别技术，并立法要求在2004年10月以前在护照上使用生物

Figure 5: The proposed framework of feature extraction based on CFBs. ‘ \otimes ’ and ‘ \oplus ’ represent the correlation operator and summation operator, respectively.

each face class. Finally, a global feature vector is obtained, whose components respectively represent the overall origin correlation outputs of all CFBs in the summed correlation output plane. In fact, the overall origin correlation output can also be derived by cumulating the inner products between the local features and a CFB. Mathematically, after obtaining a set of CFBs for all classes, each component in a global feature vector $f = (f[1], f[2], \dots, f[C])^T$ can be obtained by

$$f[c] = \sum_{m=1}^M h_{m,c}^T x_m \quad (c = 1, \dots, C), \quad (12)$$

where $\{h_{1,c}, h_{2,c}, \dots, h_{M,c}\}$ is the CFB for class c ; x_m is the raw feature vector of the m -th face subregion; C is the dimension of the global feature vector (which is equal to the number of face classes in the training set) and M is

the number of face subregions in a face image.

3.4. Classification Rule

After the feature extraction step for both training set and test set, we need to design a classifier for final classification. Note that the design process of a CFB is to produce a correlation peak only for the authentic samples for the class of interest, which means that the maximal value criterion, i.e., the class index of the maximal component in the feature vector, can be used as the classification rule. Thus the label of a test sample can be given according to

$$Label(y) = \arg \max_{i=1, \dots, C} (y[i]), \quad (13)$$

where $y = (y[1], y[2], \dots, y[C])^T$ is the extracted feature vector corresponding to the test face image.

On the other hand, the cosine similarity measure based nearest neighbor classifier can also be employed for classification. The cosine similarity measure is shown as follows:

$$Cos(y_1, y_2) = \frac{y_1^T y_2}{\|y_1\| \cdot \|y_2\|}, \quad (14)$$

where $\|\cdot\|$ represents the L_2 norm. The cosine similarity measure calculates the angle between two vectors and is not affected by their magnitudes.

The cosine similarity measure based nearest neighbor classifier is widely used in face recognition [32, 33]. In [20], it has been shown that the cosine similarity measure performs better than both L_1 norm and L_2 norm distance measures in most face recognition experiments. One reason is that [33], when an unseen sample in the test set is projected onto the feature space, the novel variations in the sample are inclined to evenly affect the projected scale on each component of the features. Thus the variations make more influence on the L_1 norm and L_2 norm distance measures (since they are affected by

the scale differences [34]) rather than the angle between two vectors (i.e., the cosine similarity measure). Therefore, the cosine similarity measure, which is invariant to changes in scale, is more effective to perform the nearest neighbor search in the feature space for face recognition.

As a matter of fact, compared with the maximal value criterion, the nearest neighbor classifier based on cosine similarity measure has two main advantages: 1) It explores the information in all components of the feature vectors in both training and test sets, which is beneficial for classification; 2) It can be applied to standard face recognition test protocols (such as FERET [35] and CAS-PEAL [36]). According to these protocols, the subjects in both gallery and probe sets can be the unseen classes (which do not exist in the training set). In such a case, each component in the extracted feature vectors obtained by MS-CFB characterizes the identity similarity between a training class and the unseen classes. Thus, the maximal value criterion is not valid for classifying the unseen classes, while the nearest neighbor classifier (comparing the feature vectors in the gallery and probe sets) can be used.

3.5. The Complete Algorithm

In the previous subsections, we have developed all ingredients for a robust face recognition algorithm. Now we put them together to yield a complete Multi-Subregion based CFB (MS-CFB) algorithm for face recognition (as detailed in Fig. 6).

3.6. Discussion

The advantages of the proposed MS-CFB algorithm over the related FE algorithms are summarized as follows. Firstly, different from traditional global-based and local-based FE algorithms, the proposed algorithm can be viewed as a hybrid algorithm, which uses local facial features to extract a

Training Stage:

Input: A training data matrix with C classes; the size of a face subregion (s); and the regularized parameter (α).

Output: A feature matrix Y_{train} of the training data.

Step 1: Divide all face images into M blocks of the same size and construct the training data matrix X_{train} (see Section 3.1);

Step 2: Do for $c = 1, \dots, C$:

2.1 Calculate the covariance matrix Σ_c via Eq. (5);

2.2 Calculate the mean value m_c via Eq. (8);

2.3 Design the correlation filter bank $g_c = (h_{1,c}; h_{2,c}; \dots; h_{M,c})$ via Eq. (11);

Step 3: Compute the feature matrix Y_{train} based on the sum of the inner products between X_{train} and $\{g_c | c = 1, 2, \dots, C\}$ via Eq. (12).

Test Stage:

Input: A test image; and a feature matrix Y_{train} of the training data.

Output: The class label of the test image.

Step 1: Divide the test face image into M blocks of the same size and construct the test data x_{test} (see Section 3.1);

Step 2: Compute the feature vector y_{test} based on the sum of the inner products between x_{test} and $\{g_c | c = 1, 2, \dots, C\}$ via Eq. (12);

Step 3: Assign the class label to the test image by using the nearest neighbor classifier with the cosine similarity measure based on y_{test} and Y_{train} .

Figure 6: The complete MS-CFB algorithm for face recognition.

global feature vector. Similar to the human perception system, a hybrid algorithm could combine the advantages of both global-based and local-based FE algorithms, and it is more robust to variations of illumination, facial expression, pose, and so on. Secondly, compared with the existing local-based FE algorithms, where classifiers are independently trained for each face sub-region, a CFB is designed by jointly optimizing multiple correlation filters

corresponding to respective face subregions at the overall origin correlation outputs. Therefore, the differences among face subregions are taken into account and the discriminative information in face subregions is more effectively exploited in MS-CFB. Thirdly, while the local FE step and the combination of local subregions are considered as two independent processes in traditional local-based FE algorithms, the proposed algorithm attempts to unify these two processes in one framework, where the local FE steps for different face subregions are integrated to produce the optimal outputs. Hence, the effectiveness of local FE is enhanced.

It is worth mentioning that a CFB becomes an unconstrained correlation filter when a whole face image without division (i.e., $M = 1$) is considered. Compared with the constrained correlation filters, such as OTF [20, 15] and OEOTF [21], the generalization capability of the unconstrained correlation filter is greatly improved since the hard constraints are removed during the filter design process. In fact, a CFB with $M = 1$ can be viewed as an unconstrained extension of an OEOTF which concentrates on the origin peaks. However, the main differences between a CFB and an OEOTF are: 1) A CFB is designed based on the spatial domain while an OEOTF is represented in the frequency domain. Therefore, traditional Fourier transforms are not required during the design process of a CFB; 2) Compared with an OEOTF that is a single filter, a CFB consists of multiple filters corresponding to different face subregions. A CFB is more robust in dealing with pose variations (by dividing a whole face image into multiple subregions) than an OEOTF.

4. Experiments

In this section, we present extensive experimental results on various public face databases to evaluate the effectiveness of the proposed algorithm. In Section 4.1, we introduce the competing algorithms and experimental set-

tings. In Section 4.2, we give the determination of the optimal parameters in MS-CFB. In Section 4.3, we demonstrate the robustness of the proposed MS-CFB algorithm against illumination variations on the Multi-PIE and FRGC face databases. In Section 4.4, we evaluate the proposed MS-CFB algorithm against pose and facial expression variations on the FERET and LFW face databases. In Section 4.5, the face recognition performance obtained by the competing algorithms on the databases with a single sample per person is presented. A comprehensive evaluation on the CAS-PEAL R1 face database is shown in Section 4.6. **The computational complexity of the proposed algorithm and the performance of the competing algorithms for automatic face recognition are given in Sections 4.7 and 4.8, respectively.** Finally, the discussion is given in Section 4.9.

4.1. The Competing Algorithms and Experimental Settings

To evaluate the performance of the proposed algorithm, we select several popular algorithms for comparisons, including the baseline Eigenface [5], Fisherface [16], OTF-based [20] and OEOTF-based [21] CFA, Sparse Representation based Classification (SRC) [3], and the state-of-the-art local-based FE algorithms including Block-FLD [37], Cascaded LDA (C-LDA) [11], Hierarchical Ensemble Classifier (HEC) [4], Block-based Bag-Of-Words (BBOW) [13], and Patch-based Collaborative Representation based Classification (PCRC) [8].

Each image in the face databases is normalized to extract a facial region that contains only the face. Specifically, the normalization for each image contains the following steps: firstly, the centers of the eyes are manually annotated; secondly, rotation and scaling transformations align the centers of the eyes to predefined locations and fixed interocular distances; finally, a face image is cropped and resized to the size of 80×88 pixels. Histogram

equalization is then applied to all face images for photometric normalization.

The reduced dimension of the PCA subspace in CFA is set to $N - 1$, where N is the number of training samples. The value of the parameter λ in SRC is set to 0.001 (which is the same as [8]). For Block-FLD, we test three different sizes of a face subregion (i.e., 10×10 , 20×20 , and 30×30) and report the best recognition results obtained with the size of 20×20 . For C-LDA, the five components encoding scheme is used. For HEC, the size of a candidate face subregion is set to a range from 16×16 to 64×64 . For PCRC, the size of a face subregion is set to 10×10 . For other parameters used in the competing algorithms, we use their default parameter settings.

After feature extraction for both training set and test set, we employ the nearest neighbor classifier for final classification. The cosine similarity measure is used for all compared algorithms. For the proposed MS-CFB algorithm, we respectively evaluate the MS-CFB (max) method (using the maximal value criterion for classification) and the MS-CFB (cos) method (using the cosine similarity measure based nearest neighbor classifier).

For all databases, a random subset (with t images per subject) is taken from each database to form the training set. The rest of the database is used as the test set. For each t , the experiments with randomly chosen subsets are performed twenty times. We report the average recognition rates as well as the standard deviations over the randomly chosen test sets as the final results. **The training set and test set for all the competing algorithms are the same for all the experiments.** In addition, the highest recognition rate for each case is shown in bold font.

In this paper, we focus on the SSS problem, which is one of the most challenging issues in face recognition [2, 8]. This problem arises when the number of the samples is smaller than the dimension of the facial feature space. In many real-world applications, the number of training samples for

each subject is very limited. Therefore, the discriminability of features under such a case is important to the final performance of a face recognition algorithm. To evaluate the effectiveness of different feature extraction algorithms to solve the SSS problem, the value of t is set to $2 \sim 5$ for all databases. In Section 4.5, we will discuss the case that the value of t is set to 1 for the SSPP problem in particular.

4.2. Determining the Optimal Parameters in MS-CFB

In MS-CFB, two parameters (i.e., the size of a face subregion s and the regularized parameter α) have an influence on the recognition accuracy. If the size of a face subregion is too large (e.g., it contains the whole face region), MS-CFB does not take advantage of local-based feature extraction. On the contrary, if the size of a face subregion is too small, MS-CFB becomes sensitive to face alignment. Similarly, the regularized parameter should also be carefully set. The purpose of regularization is to reduce the high variance related to the estimation of the covariance matrix [38], which is caused by the SSS problem.

To determine the optimal values of these two parameters (i.e., s and α) for MS-CFB, we use the AR database [39] for evaluation. The AR database contains over 4,000 face images of 126 subjects (70 men and 56 women). The AR database characterizes the divergence from ideal conditions by incorporating various facial expressions (neutral, smile, and scream), illumination changes (left light on, right light on, and both sides' light on), and occlusion modes. It has been used as a testbed to evaluate the face recognition algorithms. A subset that contains 120 subjects (each subject has 14 images) with only facial expression and illumination changes is used in our experiments (see Fig. 7 for some examples).

Fig. 8 shows the recognition rates obtained by MS-CFB (with the cosine



Figure 7: The face images of one subject on the AR database.

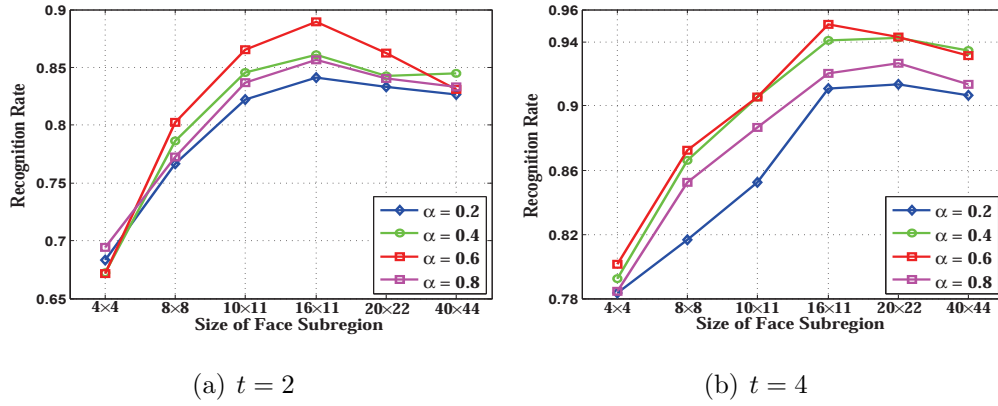


Figure 8: The recognition rates obtained by MS-CFB over different sizes of a face subregion and different values of α under $t = 2$ and $t = 4$ on the AR database.

similarity measure) over different sizes of a face subregion (including 4×4 , 8×8 , 10×11 , 16×11 , 20×22 , and 40×44) and different values of α (including 0.2, 0.4, 0.6, and 0.8) under $t = 2$ and $t = 4$ on the AR database. We can observe that when the size of a face subregion is very small (e.g., 4×4), the recognition rate is low. This is because that a face region is divided into too many subregions, which over-segments meaningful facial features (such as eyes and nose) that are critical for recognition. The recognition rates increase when the size of a face subregion becomes larger. The recognition

rate achieves the highest when the size of a face subregion is 16×11 , while the recognition rate begins to decrease for larger subregion sizes (e.g., 20×22 and 40×44), which is caused by the sensitivity of large face subregions to variations of facial expression and illumination. The value of the regularized parameter α also affects the recognition accuracy of MS-CFB. When $\alpha = 0.6$, MS-CFB achieves the best results compared with the other values of α . Therefore, we choose the size of a face subregion to be 16×11 and the value of α to be 0.6 for MS-CFB in all following experiments.

4.3. Robustness to Illumination Variations

One of the most fundamental challenges in face recognition is significant facial appearance variations due to illumination changes. In this section, we evaluate the performance of the proposed algorithm against illumination variations on two popular face databases, i.e., the Multi-PIE database [40] and the FRGC database [41].

The Multi-PIE database contains more than 750,000 images of 337 subjects captured in four sessions with variations in pose, facial expression, and illumination. A subset that contains 68 subjects (each subject has 22 images) with various illumination changes is used. *Specifically, we use the frontal pose images (i.e., the c27 subset) under 11 different illumination conditions (i.e., f01, f03, f05, f07, f09, f11, f13, f15, f17, f19, f21) with the ambient lights on/off. Fig. 9 shows the face images of one subject on the Multi-PIE database.* The FRGC (Face Recognition Grand Challenge) database consists of controlled images, uncontrolled images and three-dimensional images for each subject. We select a subset containing 6,000 images of 300 subjects (20 images for each subject) from the FRGC database. The face images in this subset are captured in both controlled and uncontrolled conditions with severe illumination variations. *Fig. 10 shows the face images of one subject*

on the FRGC database used in our experiments.



Figure 9: The face images of one subject on the Multi-PIE database.



Figure 10: The face images of one subject on the FRGC database.

Tables 1 and 2 show the average recognition accuracies obtained by the different algorithms on the Multi-PIE and FRGC databases, respectively. From these tables, we can see that the proposed MS-CFB (cos) algorithm consistently achieves better recognition accuracies than the other competing algorithms. Compared with MS-CFB (max), MS-CFB (cos) improves the recognition rates by about 4% \sim 5%, which demonstrates the advantages of using the cosine similarity measure as a metric. SRC obtains better results than Block-FLD in Multi-PIE and FRGC, which shows that SRC is more robust in dealing with illumination variations. Block-FLD constructs multiple training patterns from a single image, but it does not consider the relationships among different face subregions. PCRC, HEC, and BBOW achieve

Table 1: The average recognition accuracies (mean% \pm std.dev.) obtained by the different algorithms on the Multi-PIE database.

Algorithm	$t = 2$	$t = 3$	$t = 4$	$t = 5$
Eigenface	72.24 \pm 1.5	78.54 \pm 1.7	82.13 \pm 1.8	85.41 \pm 1.7
Fisherface	76.79 \pm 1.1	86.63 \pm 1.3	88.95 \pm 1.4	92.07 \pm 1.5
CFA (OTF)	83.15 \pm 0.8	88.05 \pm 0.8	90.17 \pm 0.6	93.10 \pm 0.5
CFA (OEOTF)	84.00 \pm 0.6	88.10 \pm 0.9	92.32 \pm 0.5	93.58 \pm 0.6
SRC	82.24 \pm 1.2	86.59 \pm 1.3	89.98 \pm 1.2	93.15 \pm 0.9
Block-FLD	81.17 \pm 1.0	82.84 \pm 1.2	88.77 \pm 1.1	89.73 \pm 1.0
C-LDA	83.25 \pm 0.9	85.77 \pm 0.8	89.95 \pm 0.9	90.07 \pm 0.8
HEC	85.56 \pm 0.8	88.74 \pm 0.6	91.41 \pm 0.8	91.11 \pm 0.6
BBOW	83.58 \pm 0.8	87.25 \pm 0.9	91.27 \pm 0.9	92.66 \pm 0.7
PCRC	86.17 \pm 0.5	90.15 \pm 0.7	92.17 \pm 0.6	93.05 \pm 0.5
MS-CFB (max)	82.51 \pm 1.1	86.24 \pm 0.9	90.05 \pm 0.8	91.17 \pm 0.6
MS-CFB (cos)	86.87\pm0.6	92.07\pm0.7	94.17 \pm0.5	96.65 \pm0.4

Table 2: The average recognition accuracies (mean% \pm std.dev.) obtained by the different algorithms on the FRGC database.

Algorithm	$t = 2$	$t = 3$	$t = 4$	$t = 5$
Eigenface	45.38 \pm 1.3	53.10 \pm 1.2	64.35 \pm 1.1	70.26 \pm 1.5
Fisherface	48.17 \pm 1.1	55.42 \pm 1.3	66.78 \pm 1.5	69.06 \pm 1.7
CFA (OTF)	54.35 \pm 0.8	62.17 \pm 0.8	65.99 \pm 0.9	73.81 \pm 1.0
CFA (OEOTF)	59.80 \pm 0.7	70.05 \pm 0.9	78.31 \pm 0.7	85.04 \pm 0.6
SRC	57.72 \pm 1.1	65.14 \pm 1.2	72.28 \pm 0.9	81.18 \pm 0.9
Block-FLD	53.14 \pm 0.8	62.28 \pm 1.3	66.77 \pm 0.9	70.20 \pm 1.0
C-LDA	55.72 \pm 1.1	66.11 \pm 0.8	72.24 \pm 1.1	76.89 \pm 1.2
HEC	57.28 \pm 1.3	66.24 \pm 1.2	71.17 \pm 1.3	75.25 \pm 1.5
BBOW	58.57 \pm 1.4	71.90 \pm 1.2	73.10 \pm 0.7	78.43 \pm 0.9
PCRC	59.02 \pm 1.0	70.02 \pm 1.0	75.65 \pm 0.6	80.11 \pm 0.5
MS-CFB (max)	59.86 \pm 1.2	70.66 \pm 1.3	78.31 \pm 1.2	85.53 \pm 1.2
MS-CFB (cos)	63.99\pm0.8	75.24\pm0.9	82.21 \pm0.5	88.58 \pm0.6

worse performance than MS-CFB (cos). The reason is that MS-CFB considers the local FE step and the combination of different face subregions as a whole, which effectively overcomes the disadvantages of the conventional fusion strategies (e.g., the majority voting used in PCRC, the weighted sum of local facial features used in HEC, and the concatenation of local features used in BBOW) employed in local-based FE algorithms.

4.4. Robustness to Pose and Facial Expression Variations

In this section, we evaluate the influence of pose and expression variations on the performance of the proposed algorithm by using two representative face databases, i.e., the FERET database [35] and the LFW database [42].

The FERET database is a standard face database for evaluating the performance of face recognition algorithms. A subset of the FERET database, which includes 1,400 images of 200 subjects (each subject has 7 images), is used. It is composed of the images whose names are marked with two-character strings: “ba”, “bj”, “bk”, “be”, “bf”, “bd”, and “bg” (see [35] for more details), as shown in Fig. 11. This subset involves challenges, such as variations in facial expression and pose. Besides, we also perform an experiment on a more realistic face database captured in unconstrained environments (i.e., the Labeled Faces in the Wild (LFW) database). The LFW database is usually used to evaluate face recognition algorithms in real scenarios. It contains the images of 5,749 different individuals collected from the web. LFW-a [43] is a version of LFW after face alignment. A subset with 150 subjects (10 images for each subject) is chosen from LFW-a. This subset involves severe variations in pose, facial expression, etc. Fig. 12 shows the sample images of one subject on the LFW database used in our experiments.

Tables 3 and 4 show the experimental results on the FERET and LFW databases, respectively. MS-CFB (cos) obtains comparable or better recog-

Table 3: The average recognition accuracies (mean% \pm std.dev.) obtained by the different algorithms on the FERET database.

Algorithm	$t = 2$	$t = 3$	$t = 4$	$t = 5$
Eigenface	53.27 \pm 3.0	60.12 \pm 2.9	65.50 \pm 2.7	70.22 \pm 2.1
Fisherface	66.63 \pm 1.8	67.79 \pm 1.7	76.23 \pm 1.6	77.54 \pm 1.3
CFA (OTF)	58.96 \pm 1.7	65.53 \pm 1.5	74.18 \pm 1.1	78.97 \pm 1.4
CFA (OEOTF)	75.27 \pm 1.5	79.92 \pm 1.6	90.02 \pm 1.3	91.50 \pm 1.3
SRC	66.21 \pm 2.1	67.14 \pm 2.2	71.16 \pm 2.5	75.36 \pm 2.1
Block-FLD	67.57 \pm 1.8	69.95 \pm 1.7	73.28 \pm 1.7	80.95 \pm 1.6
C-LDA	68.83 \pm 2.1	70.17 \pm 2.3	75.36 \pm 2.4	83.27 \pm 2.3
HEC	71.72 \pm 1.8	74.92 \pm 1.7	80.38 \pm 1.8	85.50 \pm 1.9
BBOW	74.15 \pm 1.6	77.42 \pm 1.2	86.00 \pm 1.5	92.34 \pm 1.5
PCRC	75.24 \pm 1.5	79.17 \pm 1.2	87.93 \pm 1.4	95.85 \pm1.3
MS-CFB (max)	75.10 \pm 1.9	81.14 \pm 1.8	90.15 \pm 1.1	92.11 \pm 1.4
MS-CFB (cos)	80.60\pm1.4	84.72\pm1.3	94.26 \pm1.2	94.93 \pm 1.1

Table 4: The average recognition accuracies (mean% \pm std.dev.) obtained by the different algorithms on the LFW database.

Algorithm	$t = 2$	$t = 3$	$t = 4$	$t = 5$
Eigenface	24.15 \pm 3.2	28.10 \pm 3.8	32.23 \pm 3.5	37.00 \pm 3.7
Fisherface	27.89 \pm 2.8	33.42 \pm 2.7	38.42 \pm 2.4	44.25 \pm 2.3
CFA (OTF)	25.27 \pm 3.5	30.17 \pm 3.9	32.17 \pm 4.0	35.24 \pm 3.5
CFA (OEOTF)	30.11 \pm 2.1	35.39 \pm 1.8	39.95 \pm 1.6	42.13 \pm 1.5
SRC	30.25 \pm 2.5	35.24 \pm 2.3	39.97 \pm 2.8	45.13 \pm 2.0
Block-FLD	32.53 \pm 2.3	36.78 \pm 2.4	40.12 \pm 1.9	45.24 \pm 1.5
C-LDA	31.10 \pm 2.2	35.41 \pm 2.1	38.82 \pm 1.5	44.99 \pm 1.3
HEC	33.24 \pm 2.3	41.78 \pm 2.2	45.80 \pm 1.5	49.72 \pm 1.9
BBOW	31.27 \pm 2.2	33.41 \pm 1.9	41.17 \pm 1.5	48.21 \pm 1.5
PCRC	38.20 \pm2.0	42.17 \pm 1.4	48.58\pm1.3	50.72 \pm 1.3
MS-CFB (max)	31.10 \pm 2.4	35.22 \pm 2.1	42.32 \pm 2.0	46.00 \pm 1.8
MS-CFB (cos)	37.17 \pm 1.8	43.10\pm1.5	47.15 \pm 1.4	52.20 \pm1.2



Figure 11: The face images of one subject on the FERET database.



Figure 12: The face images of one subject on the LFW database.

nition rates than the other algorithms. Particularly, the performance of MS-CFB (cos) increases significantly when more training sample are used. MS-CFB (cos) improves the discriminability of features by adopting the unconstrained form (which is beneficial for learning the underlying classification boundary) during the design process of a CFB. The recognition accuracies obtained by CFA (OTF) and CFA (OEOTF) are lower than those obtained by MS-CFB (cos). This is due to the fact that the usage of the whole face region makes CFA sensitive to pose variations. In contrast, MS-CFB (cos) alleviates this problem by using multiple face subregions. Furthermore, BBOW obtains lower recognition rates than HEC and PCRC on the LFW database, which indicates that BBOW cannot effectively capture the intrinsic discriminative information when the training set contains variations in pose and facial expression.

Compared with the recognition results on other databases, MS-CFB (cos) obtains lower accuracies on the LFW database. There are two main reasons: 1) After the multi-subregion division procedure, some face subregions contain the surrounding background (mainly caused by pose changes), which

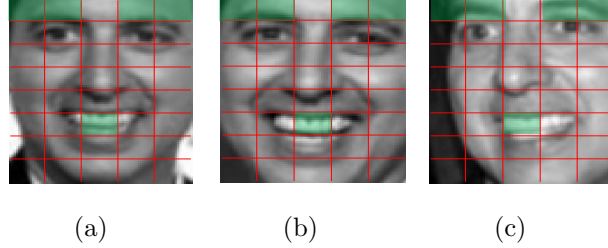


Figure 13: Multi-block division of the same subject with different poses based on our face alignment (an image is divided into 5×8 blocks and the size of each block is 16×11 pixels). (a) and (b) are both frontal face images while (c) is a face image with a large pose variation. Note that the blocks marked with green in (a) and (b) are aligned, while the marked blocks in (c) are not well-aligned with the ones in (a) and (b).

decreases the discriminability of features extracted by our algorithm (note that MS-CFB is based on the sum of the correlation outputs from all face subregions); 2) The mismatching of face subregions between training samples and test samples can occur when dealing with large pose variations. See Fig. 13 for an example. In our experiments all face images are aligned only according to the manually annotated eye positions, as in [21, 34]. When handling the frontal face images, most face subregions between training samples and test samples, corresponding to specific facial structures (such as eyes, mouth), can be aligned, which makes our algorithm work well. However, when matching face images with large pose variations, the performance of our algorithm drops. This is because the face alignment method employed in our work is not effective enough so that the blocks with the same spatial layout are not well-aligned in this case, which leads to low correlation values between face subregions and the corresponding correlation filters. Therefore, a more effective face alignment technique can improve the performance of

our algorithm, especially for handling images with large pose variations.

4.5. Face Recognition on Databases with a Single Sample Per Person

In this section, we test the performance of the competing algorithms on all above-mentioned databases with a Single training Sample Per Person (SSPP) [2, 44] (which is an extreme case of the SSS problem that severely challenges conventional face recognition algorithms). In such a case, supervised learning techniques, such as LDA [16], may not be applicable since the intra-subject information cannot be obtained from one training sample. One possible solution is to use a generic training set. For instance, Su et al. [45] proposed an Adaptive Generic Learning (AGL) algorithm, which is specially designed for solving the SSPP problem by using a generic training set. Kan et al. [46] developed an Adaptive Discriminant Analysis (ADA) algorithm, where the within-class scatter matrix of each single sample is inferred by using only a limited number of the nearest neighbors in the generic training set. Recently, the image partitioning based algorithms become popular for solving the SSPP problem. Lu et al. [47] proposed a novel Discriminative Multi-Manifold Analysis (DMMA) algorithm by learning discriminative features from image patches. Therefore, AGL, ADA and DMMA are employed as the competing algorithms in our experiments. When we evaluate the performance of AGL (or ADA) on one database, all the other databases are used to constitute the generic training set in AGL (or ADA). For the other algorithms, we only use a single sample per person for training. Note that since Fisherface [16] (based on LDA) cannot deal with the SSPP problem, its performance is not reported in this section.

Table 5 shows the average recognition accuracies obtained by the competing algorithms in dealing with the SSPP problem. Among the competing algorithms, MS-CFB (cos) obtains comparable results on most databases.

Table 5: The average recognition accuracies (mean% \pm std.dev.) obtained by the different algorithms for the SSPP problem.

Algorithm	AR	Multi-PIE	FRGC	FERET	LFW
Eigenface	35.77 \pm 3.5	50.15 \pm 3.5	22.42 \pm 4.1	33.70 \pm 3.8	11.13 \pm 3.8
CFA (OTF)	38.54 \pm 3.4	55.54 \pm 2.5	40.17 \pm 3.8	31.00 \pm 3.5	13.21 \pm 2.8
CFA (OEOTF)	53.27 \pm 2.9	58.10 \pm 2.1	43.50 \pm 3.1	55.27 \pm 3.0	16.17 \pm 2.6
SRC	45.27 \pm 3.2	57.89 \pm 1.8	38.28 \pm 3.3	43.82 \pm 3.3	15.26 \pm 2.7
Block-FLD	48.81 \pm 2.4	56.17 \pm 1.4	45.17 \pm 3.0	50.47 \pm 2.8	18.78 \pm 2.5
AGL	55.41 \pm 3.4	60.95 \pm 1.7	50.20 \pm 2.8	55.14 \pm 1.3	15.11 \pm 3.2
ADA	60.18 \pm 3.0	60.16 \pm 1.9	51.76 \pm 2.7	60.11 \pm 62	19.32 \pm 3.0
DMMA	67.24\pm2.0	62.55 \pm 1.6	53.15\pm2.7	65.24 \pm 2.5	22.17\pm2.8
BBOW	64.21 \pm 2.5	55.98 \pm 1.8	46.31 \pm 2.7	60.52 \pm 3.0	17.37 \pm 3.2
PCRC	65.40 \pm 2.3	61.11 \pm 1.6	48.94 \pm 3.2	64.25 \pm 2.2	22.14 \pm 2.8
MS-CFB (max)	61.21 \pm 2.9	57.72 \pm 2.5	45.30 \pm 2.4	61.78 \pm 2.1	16.66 \pm 2.2
MS-CFB (cos)	66.13 \pm 2.2	62.81\pm1.5	52.74 \pm 2.8	66.60\pm2.1	21.15 \pm 2.9

Specifically, MS-CFB (cos) outperforms most of the compared local-based algorithms, such as Block-FLD, BBOW, and PCRC. Furthermore, it obtains comparable performance with the recently proposed DMMA algorithm which considers the local face subregions of each subject as a manifold. The reason why our algorithm is comparable to these state-of-the-art algorithms even if only raw data of local face subregions is used is that our algorithm extracts global features by effectively combining local features in an integrated framework, while others extract local features independently. Furthermore, compared with the AGL and ADA algorithms, which additionally use a generic training set, MS-CFB (cos) still achieves better performance, which clearly demonstrates the desirable classification ability of the proposed algorithm. It is also interesting to observe that MS-CFB (cos), DMMA, and PCRC obtain better recognition results than AGL and ADA in most databases.

Note that the results obtained by some competing algorithms (such as

DMMA [47], PCRC [8], AGL [45], and ADA [46]) in our experiments are different from the reported results. This is because that the experimental settings in our paper and the original papers are different. For instance, in the original papers [47, 8], DMMA used the standard FERET evaluation protocol, while PCRC used more than 2 images per person for training. In contrast, for DMMA and PCRC, we only use a single sample per person for training in our paper. In addition, in the original papers [45, 46], AGL (or ADA) uses a generic training set that is similar to the test set. However, when we evaluate the performance of AGL (or ADA) on one database in this paper, all the other databases are used to constitute the generic training set (which is significantly different from the test set) for AGL (or ADA). Hence, the accuracies of AGL and ADA are lower than those reported in the original papers. How to choose a proper and representative generic training set still needs further investigation for AGL and ADA.

4.6. Face Recognition on CAS-PEAL R1 with Unseen Subjects

To evaluate the generalization capability of the proposed algorithm, we use the CAS-PEAL R1 face database for evaluation. The CAS-PEAL R1 database contains three types of datasets, i.e., the training set, gallery set and probe set. The training set contains 300 subjects and each subject has 4 images. The gallery set includes 1,040 images of 1,040 subjects (each subject has one image captured under a normal condition). The CAS-PEAL R1 database contains six probe sets under six different conditions: accessory, age, background, distance, expression, and lighting. All images that appear in the training set are excluded from the probe sets and the probe subjects may not exist in the training set. We employ the evaluation protocol introduced in [36]. Here only the training set is used to train all of the algorithms. The details of the CAS-PEAL R1 database are described in Table 6. Fig. 14 shows

the face images of two subjects on the CAS-PEAL R1 training set. Among the competing algorithms, SRC and PCRC are infeasible to deal with the case that the probe subjects are the unseen subjects in the probe sets, because a test image is represented as a linear combination of the training samples for these two algorithms. In addition, MS-CFB (max) is not evaluated, since it is not valid for classifying unseen subjects.



Figure 14: The face images of two subjects on the CAS-PEAL R1 training set.

Table 6: The datasets used in the CAS-PEAL R1 evaluation protocol.

Datasets	Training set	Gallery set	Probe set (frontal)					
			Accessory	Age	Background	Distance	Expression	Lighting
No. of Images	1,200	1,040	2,285	66	553	275	1,570	2,243

The recognition rates obtained by the different algorithms on the CAS-PEAL R1 database are given in Table 7. It can be seen that MS-CFB (cos) achieves the recognition rates with at least 6% higher (on an average) than the other competing algorithms. Fisherface obtains the worst recognition rates (which are much lower than the recognition rates obtained by Eigenface). The generalization capability of Fisherface is poor because the number of training samples for each class is small. BBOW obtains much worse performance than HEC and C-LDA. The reason is that the codewords learned in

Table 7: The recognition rates (%) obtained by the different algorithms on the CAS-PEAL R1 database .

Algorithm	Accessory	Age	Background	Distance	Expression	Lighting	Average
Eigenface	59.39	57.58	95.84	93.09	73.69	10.16	51.00
Fisherface	45.95	33.33	87.70	77.45	61.34	4.95	40.67
CFA (OTF)	53.52	56.06	94.58	92.00	67.83	15.78	49.41
CFA (OEOTF)	73.39	66.67	98.19	98.18	83.31	30.14	64.62
B-FLD	65.43	63.64	90.60	93.82	75.92	23.09	57.29
C-LDA	69.80	69.70	94.03	94.91	76.05	24.92	59.71
HEC	70.68	71.21	94.21	96.36	82.04	35.62	64.86
BBOW	60.18	57.58	92.59	94.55	71.21	20.33	53.76
MS-CFB (cos)	75.49	75.76	97.29	97.82	88.28	42.71	70.45

the training set are not representative (note that some subjects in the probe sets are different from those in the training set). MS-CFB (cos) achieves the highest recognition rates on the ‘*Accessory*’, ‘*Age*’, and ‘*Expression*’ probe sets. In particular, for the most difficult ‘*Lighting*’ probe set, MS-CFB (cos) significantly improves the recognition accuracy (it achieves the recognition rate of 70.45%), while Fisherface only obtains the recognition rate of 4.95%. In short, these experimental results on the CAS-PEAL R1 database show that the CFBs learned on the training set can classify unseen subjects well in the proposed MS-CFB.

4.7. Computational Complexity of the Proposed Algorithm

We compare the computational time of the proposed MS-CFB algorithm with that of some representative feature extraction algorithms, including Eigenface, Fisherface, CFA (with OTF and OEOTF), and PCRC. All the computational time is reported on a workstation with 2 Intel Xeon E5620 (2.40GHz) CPUs (only one core is used) on the MATLAB platform. Table

8 shows the computational time spent on the training and test (recognition) stages by these algorithms on the CAS-PEAL R1 database.

Table 8: Comparisons of the computational time (in seconds) used by the competing algorithms on the CAS-PEAL R1 database.

Algorithm	Training time	Recognition time
Eigenface	51.41	70.61
Fisherface	83.79	20.62
CFA (OTF)	522.74	32.88
CFA (OEOTF)	202.78	30.41
PCRC	65.27	23.80
MS-CFB	3134.21	82.64

As shown in Table 8, the computational time of the proposed MS-CFB used for training is higher than that of the other algorithms. However, the computational time of MS-CFB used for recognition is comparable to that of the other algorithms (and the proposed MS-CFB achieves more accurate recognition rates when it is compared with these competing algorithms on the CAS-PEAL R1 database). As the training stage is usually performed offline, the computational complexity of the proposed algorithm will not constrain its applications to real-world tasks.

4.8. Automatic Face Recognition

In the above experiments, the facial part in each image is cropped and resized into the size of 80×88 based on manually annotated eye positions. However, in many real-world applications, a robust face recognition system should be a fully automatic system (it is not realistic to manually annotate the centers of eyes for each test face image). Hence, in this section, we

evaluate the performance of all the competing algorithms in the applications of automatic face recognition. To be specific, we manually align and crop each face image in the training set and automatically detect, crop, and resize each image in the test set by using a popular face detector [48] and an automatic eye detector [49]. A subset (includes 1,400 images of 200 individuals) of the FERET database is used for comparisons. The experimental settings used are the same as those in Section 4.4. Here, the number of training samples for each subject t is set to 3. Fig. 15 shows the average recognition accuracies when manual annotation and automatic detection are respectively applied.

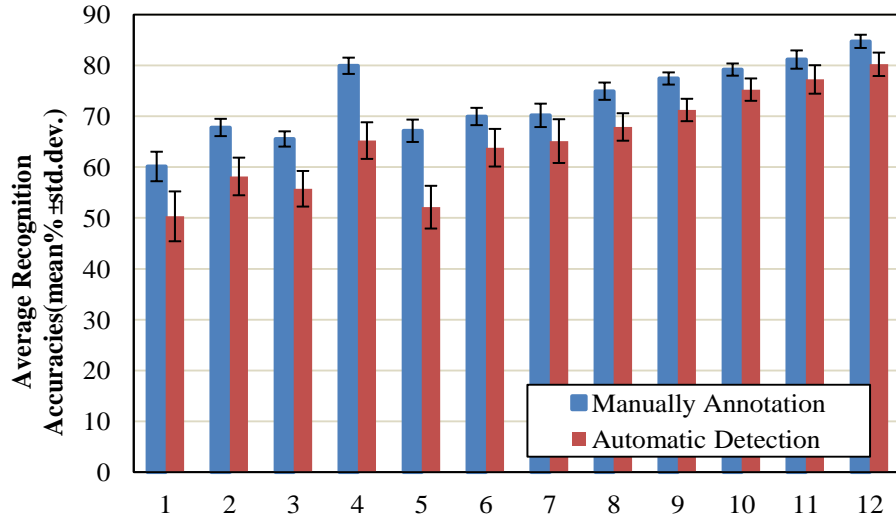


Figure 15: The average recognition accuracies (mean% \pm std.dev.) when manual annotation and automatic detection are respectively applied. Methods 1-12 correspond to Eigenface, Fisherface, CFA(OTF), CFA (OEOTF), SRC, Block-FLD, C-LDA, HEC, BBOW, PCRC, MS-CFB (max), MS-CFB (cos), respectively.

From Fig. 15, we can observe that the accuracy of automatically detected positions of the centers of eyes affects the face recognition performance of all

the competing algorithms. This is due to the fact that there usually contain some spatial misalignments caused by location errors in the automatically detected face images, which leads to a negative influence on the recognition accuracy. Experimental results have verified the degrade of the recognition performance (about a 3% \sim 10% drop) with automatic detection of the centers of eyes. However, the local-based algorithms (such as Block-FLD, BBOW, PCRC, and the proposed MS-CFB) are more robust against spatial misalignments than the global-based algorithms (such as Eigenface, CFA, and SRC). This is because the local-based algorithms can alleviate the misalignment effects by partitioning a face image into smaller face subregions. In particular, experimental results have shown that the proposed MS-CFB gives the smallest drop on the recognition accuracy, since it effectively combines local features in an integrated framework.

4.9. Discussion

From the above-mentioned experimental results, we can see that the proposed MS-CFB with the cosine similarity measure can achieve better recognition accuracies than most competing algorithms to handle the SSS problem. There are two reasons why MS-CFB achieves superior performance: 1) MS-CFB partitions each face image into multi-subregions and an effective learning algorithm (i.e., CFB) is applied to explore discriminative local features which are more robust to variations caused by facial expression, illumination, and pose; 2) MS-CFB extracts discriminative features in a class-specific manner, while the others extract features in a generic way.

It is worth remarking upon the performance comparisons between different algorithms.

(1) Eigenface, which is based on PCA, extracts the most representative features in terms of the minimal mean squared error. However, PCA is not

optimal for the classification problem, which results in less effectiveness of Eigenface in face recognition. On the contrary, MS-CFB emphasizes the correlation outputs for authentic samples while suppressing the outputs for impostor samples. Therefore, MS-CFB can extract discriminative features which effectively distinguish different classes.

(2) The projection vector obtained by Fisherface discriminates all classes. One problem of Fisherface is that it is not able to effectively discriminate two classes close to each other since large class distances are often overemphasized (which is also known as the class separation problem [50]). In contrast, the projection vector of MS-CFB focuses on the separation between one specific class and all the other classes. As a result, MS-CFB can alleviate the class separation problem.

(3) Compared with CFA, where the correlation filter is designed in the frequency domain, the CFB used in MS-CFB only employs the feature representation in the spatial domain which improves the computational efficiency by removing the traditional Fourier transforms during the design process of a CFB. Furthermore, different from the commonly used OTF and OEOTF (which are the constrained correlation filters), the design of a CFB removes the hard constraints by using the unconstrained form so as to increase the generalization capability of the filter bank.

(4) While most FE algorithms are required to select the optimal reduced dimension (ORD) [51], MS-CFB does not need to determine the ORD, thus improving the convenience. This is because the dimension of the feature vector obtained by MS-CFB is a fixed value (which is equal to the number of classes in a training set). Moreover, compared with popular local-based FE algorithms (such as HEC and PCRC), where the local FE step and the combination of local subregions are performed as two independent processes, MS-CFB unifies these two processes in an effective framework.

5. Conclusions and Future Work

In this paper, we have presented an effective feature extraction algorithm called MS-CFB and applied it to the task of face recognition. MS-CFB unifies the local feature extraction step and the combination of different face subregions in an integrated framework. The key idea of MS-CFB is that, instead of extracting local features independently for each face subregion, the local feature extraction steps for different face subregions are combined to give optimal overall correlation outputs. We have evaluated MS-CFB under different conditions, including variations in illumination, facial expression, and pose, as well as dealing with the SSPP problem. Experimental results have shown that MS-CFB outperforms most state-of-the-art feature extraction algorithms, such as SRC, HEC, and PCRC, on popular face databases for solving the SSS problem.

As mentioned in our experiments, the multi-block division strategy (based on rectangle blocks) used in the proposed algorithm cannot handle face recognition with large pose variations well due to the fact that all face images are manually aligned according to the eye positions. Recent work has demonstrated that the usage of irregular subregions can be helpful to improve face recognition performance. For instance, Kumar et al. [6] defined 10 subregions with different shapes (e.g., rectangles, eclipses, polygons, etc.) corresponding to functional parts of a face (such as the nose, mouth, eye) in recognition. Hence, how to design adaptive face subregions to improve the performance of MS-CFB under large pose variations is an interesting direction of our future work. In addition, we are interested in extending the idea of MS-CFB to the task of facial expression recognition and other biometric recognition applications.

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